



Object-Oriented Programming with Java



Recitation No. 3 (Class Verification)

BoundedVersionedString

- A VersionedString with a bounded capacity
- Abstraction Function:

$$A : BVS \rightarrow \{\phi\} \cup S \cup S \times S \cup \dots \cup S^{capacity}$$

where:

- $BVS = \{vs \mid vs \text{ is a BoundedVersionedString state}\}$
- $S = \{s \mid s \text{ is a String}\}$

$$vs \in BVS \xrightarrow{A} \begin{cases} \phi \\ s \in S \\ (s_1, s_2) \in S \times S \\ (s_1, s_2, s_3) \in S \times S \times S \end{cases}$$

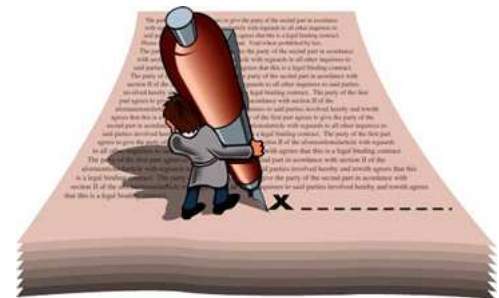
Method Specification

```
public class BoundedVersionedString {  
    public BoundedVersionedString(int capacity) {...}  
    public void add(String s) {...}  
    public int length() {...}  
    public String getLastVersion() {...}  
    public String getVersion(int i) {...}  
}
```

The Contract

Pre/Post Conditions

- BoundedVersionedString(int capacity):
 - Requires:
 - capacity > 0
 - Ensures:
 - nothing



The Contract

Pre/Post Conditions (cont.)

■ void add(String s):

- Requires:

$s \neq \text{null}$

- Ensures:

$A(\text{old}) = \phi \Rightarrow A(\text{new}) = (s)$

$A(\text{old}) = (s_1, s_2, \dots, s_{k \geq 1}) \Rightarrow A(\text{new}) = \begin{cases} (s_1, s_2, \dots, s_k, s) & \text{if } k < \text{capacity} \\ (s_2, s_3, \dots, s_k, s) & \text{if } k = \text{capacity} \end{cases}$

The Contract

Pre/Post Conditions (cont.)

■ `int length()`:

- Requires:

nothing

- Ensures:

$A(new) = A(old)$

Since `length()` is a query

$returned\ value = \begin{cases} 0 & \text{if } A(old) = \phi \\ k & \text{if } A(old) = (s_1, \dots, s_{k \geq 1}) \end{cases}$

The Contract

Pre/Post Conditions (cont.)

■ String getVersion(int i):

- Requires:

$$A(\text{this}) = (s_1, s_2, \dots, s_{k \geq i \geq 1})$$

- Ensures:

$$A(\text{new}) = A(\text{old})$$

$$A(\text{old}) = (s_1, \dots, s_{k \geq i \geq 1}) \Rightarrow \text{returned value} = s_i$$

The Contract

Pre/Post Conditions (cont.)

■ String getLastVersion():

- Requires:

$$A(\textit{this}) \neq \phi$$

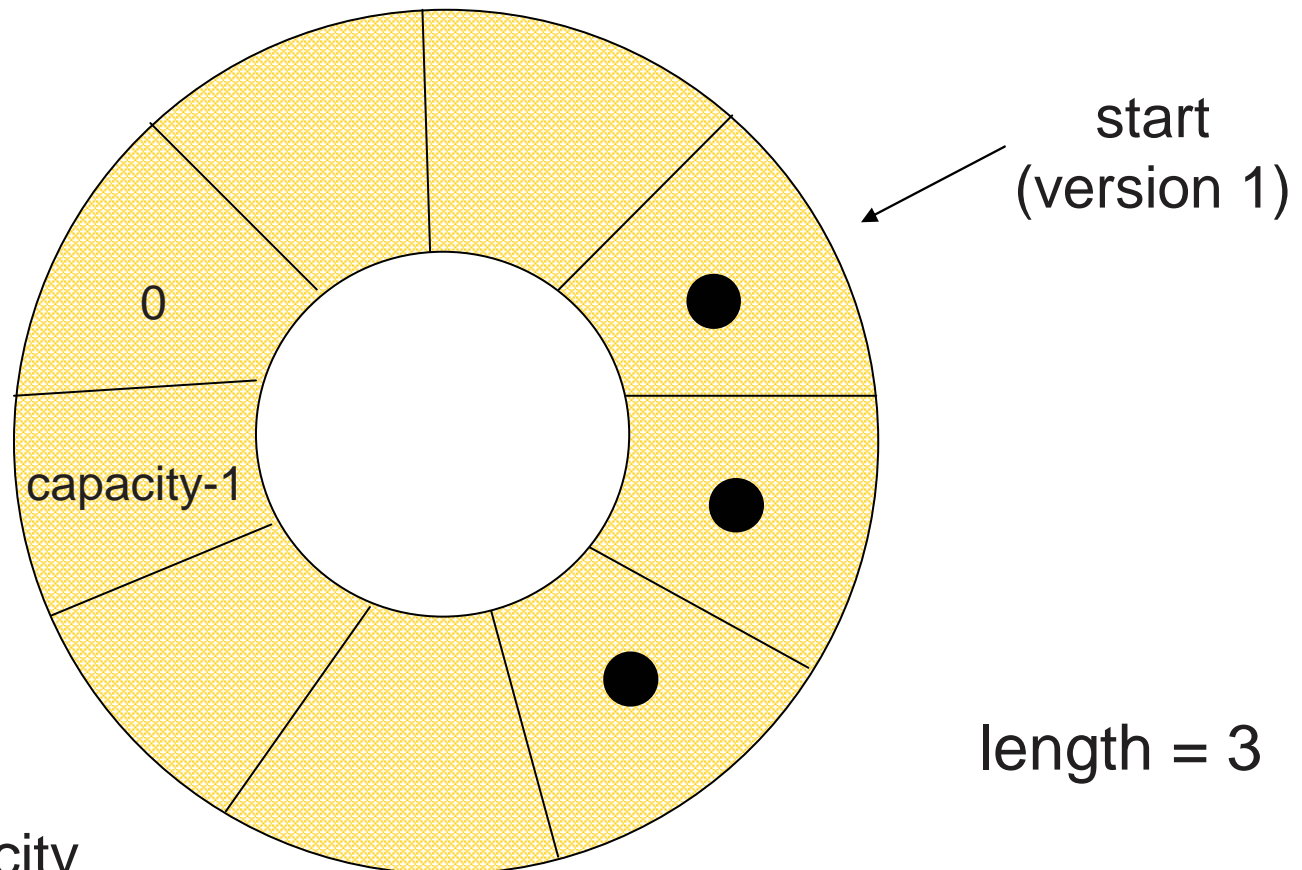
- Ensures:

$$A(\textit{new}) = A(\textit{old})$$

$$A(\textit{old}) = (s_1, \dots, s_k) \Rightarrow \textit{returned value} = s_k$$

Implementation

- Based on a circular array



Array size = capacity

Implementation (cont.)

Fields

// Stores the remembered versions
private String[] **versions** ;

// The maximum number of versions to remember
private int **capacity**;

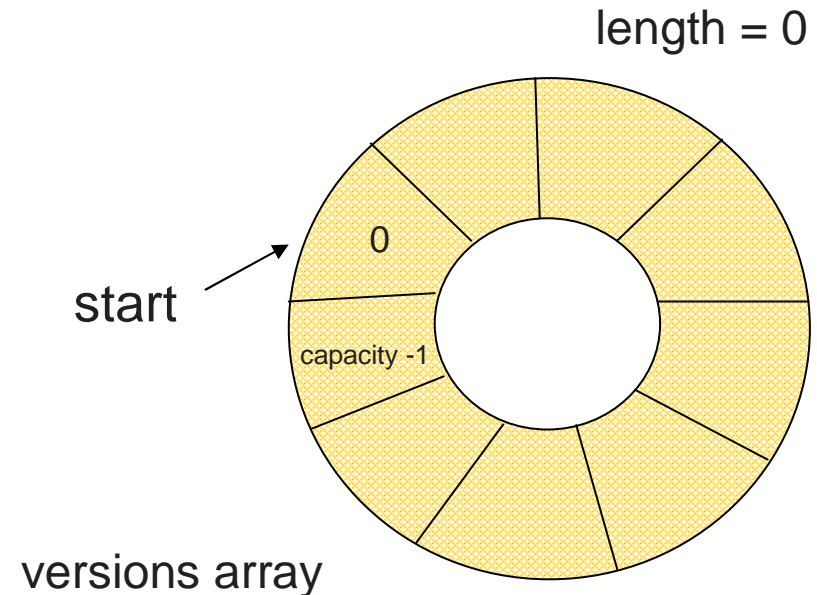
// The actual number of remembered versions
private int **length** = 0;

// The position of the oldest remembered version
private int **start** = 0;

Implementation (cont.)

Constructor

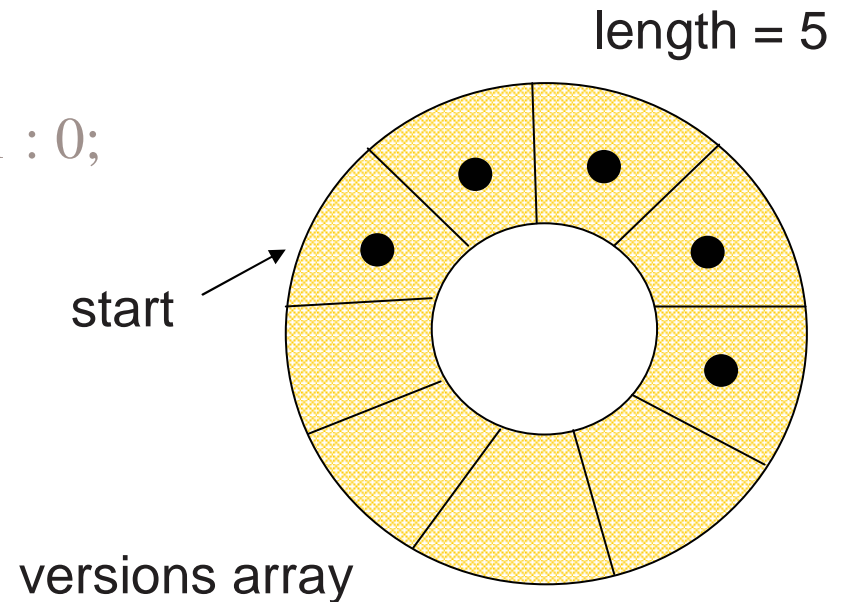
```
public BoundedVersionString(int capacity) {  
    this.capacity = capacity;  
    versions = new String[capacity];  
}
```



Implementation (cont.)

Command

```
public void add(String s) {  
    int pos = (start + length) % capacity;  
    versions[pos] = s;  
  
    if ((length > 0) && (start == pos)) {  
        start = (start+1) % capacity;  
    }  
  
    length += (length < capacity) ? 1 : 0;  
}
```



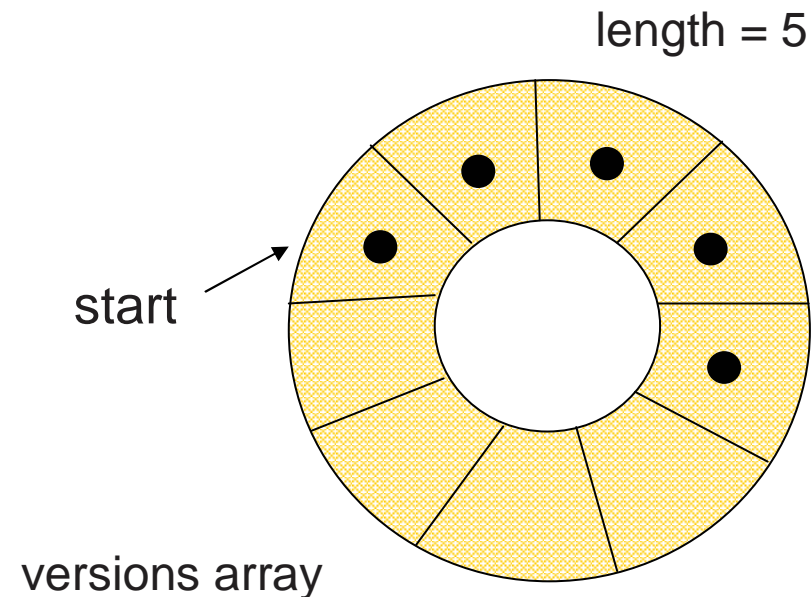
Implementation (cont.)

Queries

```
public int length() {  
    return length;  
}
```

```
public String getVersion(int i) {  
    return versions[(start+i-1)%capacity];  
}
```

```
public String getLastVersion() {  
    return getVersion(length());  
}
```



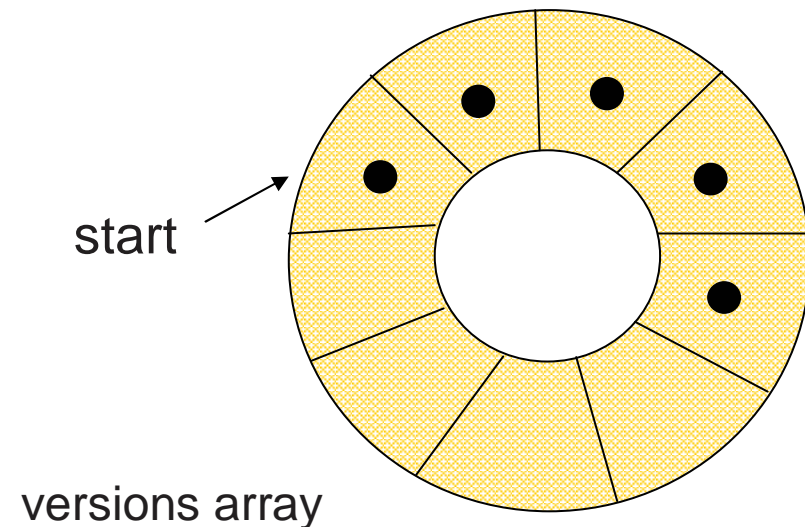
Abstraction Function Definition

$$A : BVS \rightarrow \{\phi\} \cup S \cup S \times S \cup \dots \cup S^{capacity}$$

where:

- $BVS = \{vs \mid vs \text{ is a BoundedVersionedString state}\}$
- $S = \{s \mid s \text{ is a String}\}$

$$A(this) = (versions [start], \dots, versions [(start + length - 1) \% capacity])$$



Representation Invariant

1. $capacity > 0$
2. $0 \leq start < capacity$
3. $length < capacity \Rightarrow start = 0$
4. $length = \begin{cases} 0 & \text{if } A(this) = \phi \\ k & \text{if } A(this) = (s_1, \dots, s_{k \geq 1}) \end{cases}$

Class Verification

■ Invariant Verification in initial state:

- $capacity > 0$ (construction precondition) ■ 1
- $0 = start < capacity$ (initial state, 1) ■ 2
- $length() = 0$ (initial state) ■ 3,4
- $A(this) = (versions[0], \dots, versions[-1]) = \emptyset$ ■

Class Verification (cont.)

- Method Verification:
 - Assume: The invariant and pre-condition are satisfied **before** the call
 - Prove: The invariant and post-condition are satisfied **after** the call
- Other Code Verification:
 - Prove: No other code in the program change the invariant.