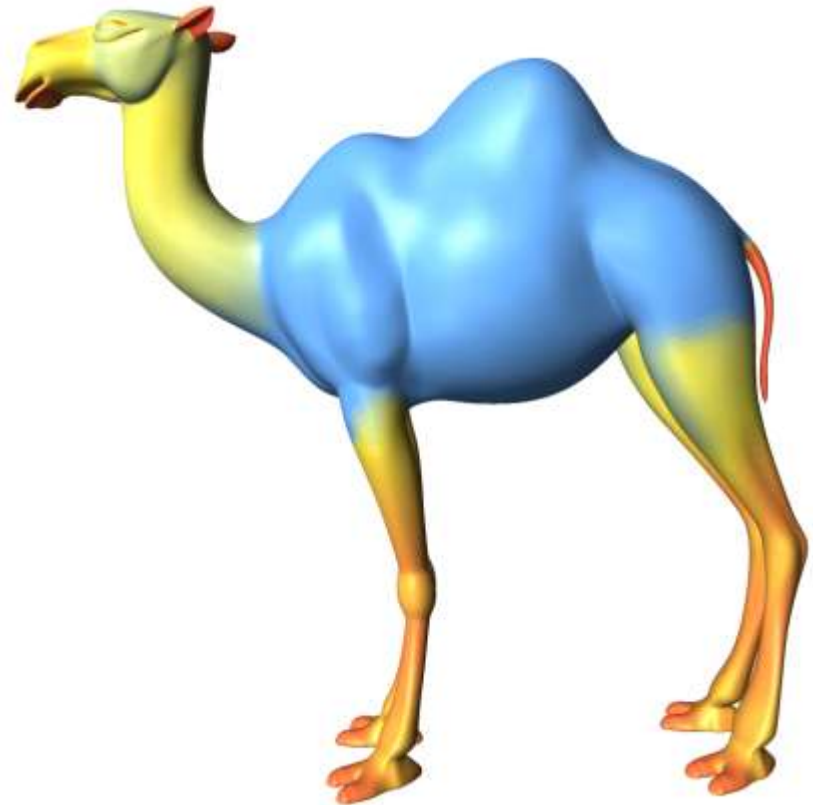


# 3D Modeling I

CG08b

Lior Shapira

Lecture 8



Based on:

Thomas Funkhouser, Princeton University

# Course Syllabus

I. Image processing

II. Rendering

**III. Modeling**

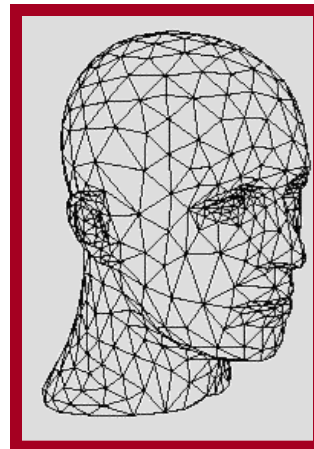
IV. Animation



**Image Processing**  
*(Rusty Coleman, CS426, Fall99)*



**Rendering**  
*(Michael Bostock, CS426, Fall99)*



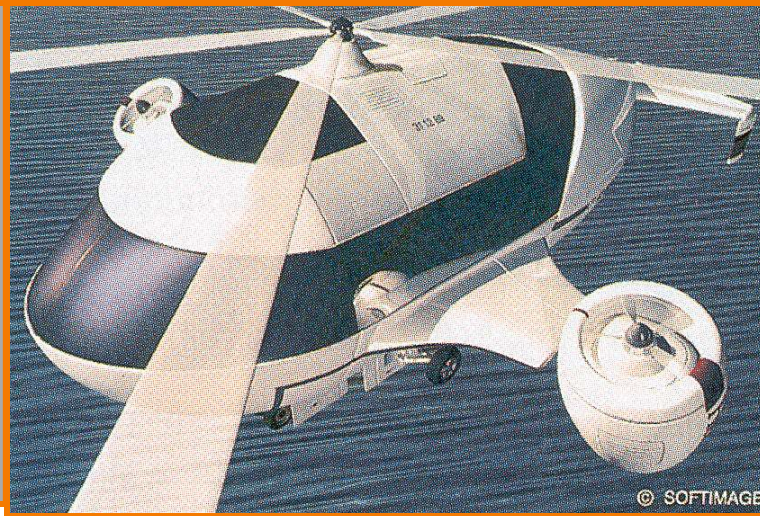
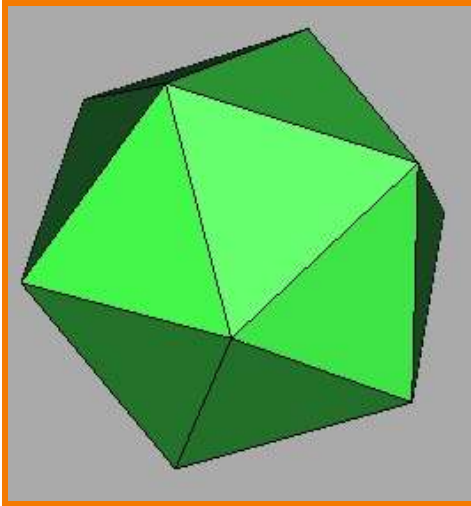
**Modeling**  
*(Dennis Zorin, CalTech)*



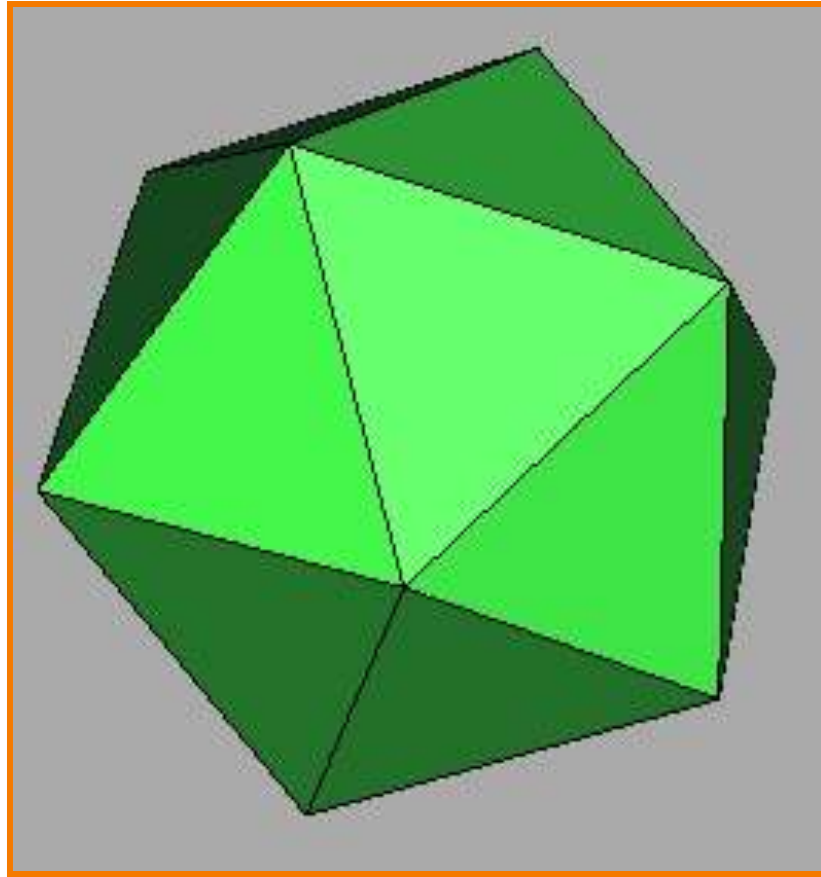
**Animation**  
*(Angel, Plate 1)*

# Modeling

- How do we ...
  - Represent 3D objects in a computer?
  - Acquire computer representations of 3D objects?
  - Manipulate computer representations of 3D objects?



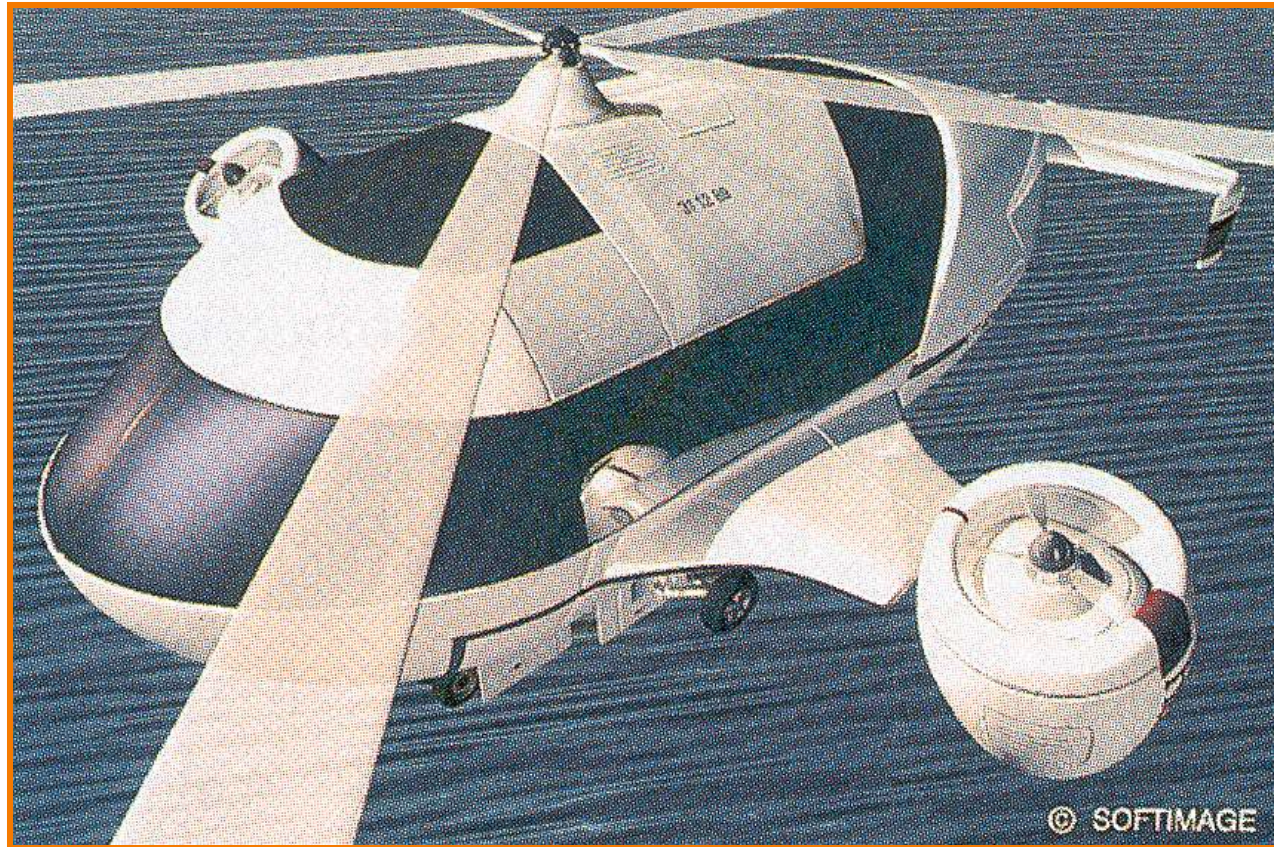
# 3D Objects



How can this object be represented in a computer?



# 3D Objects



H&B Figure 10.46

This one?

# 3D Objects

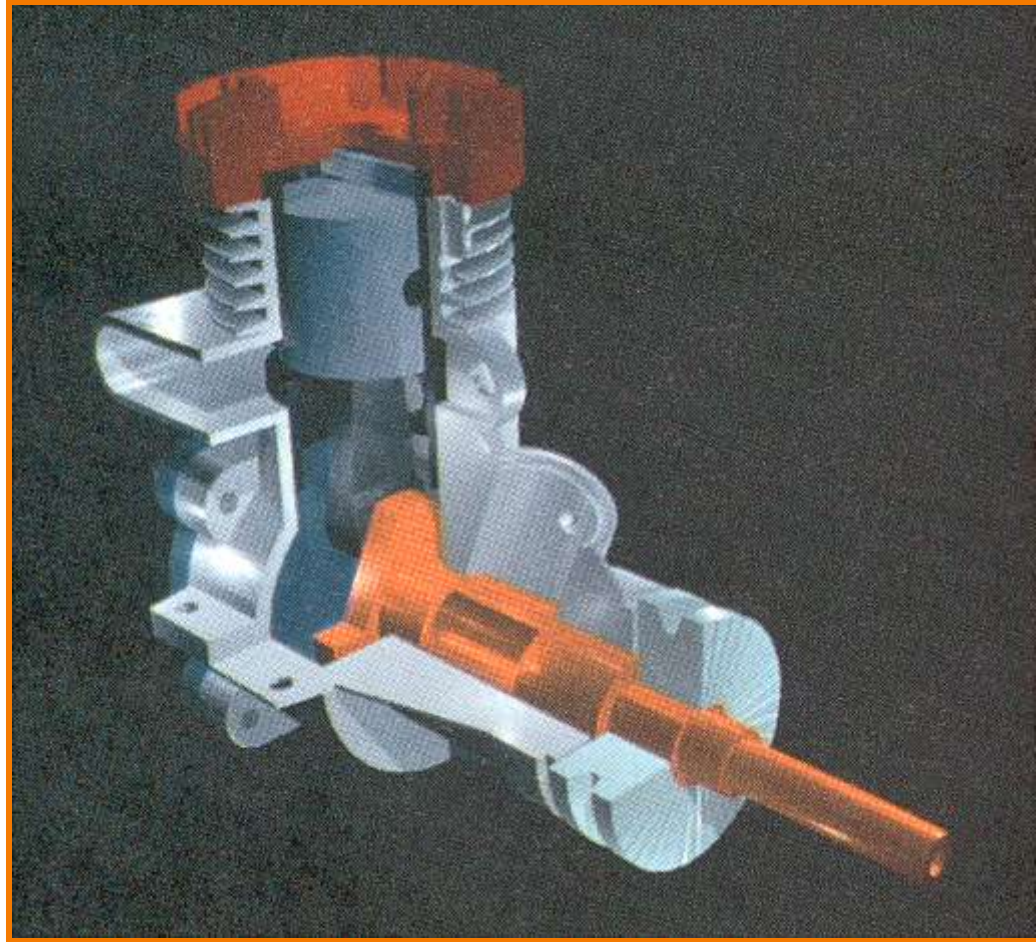


Stanford Graphics Laboratory

How about this one?



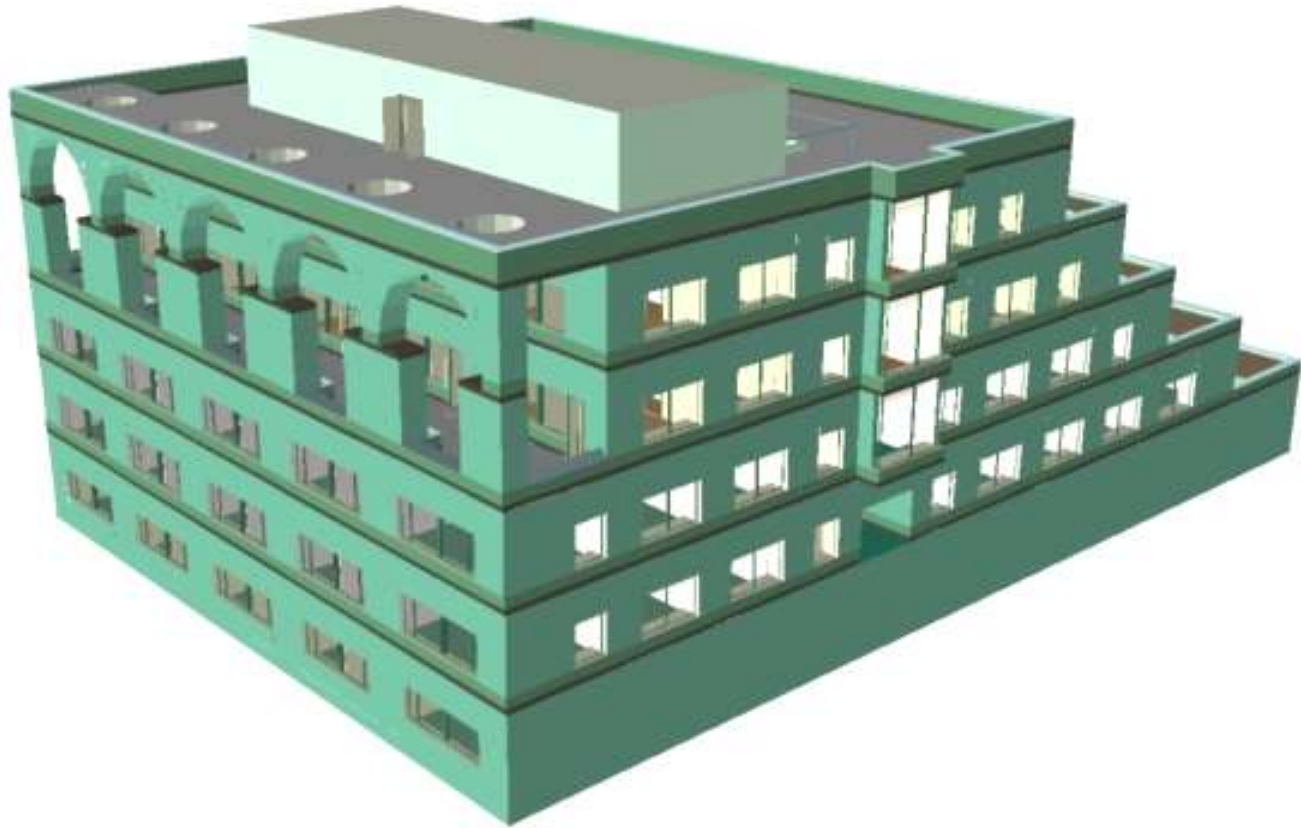
# 3D Objects



This one?

H&B Figure 9.9

# 3D Objects



This one?



# 3D Object Representations

- Points
  - Point cloud
  - Range image
- Surfaces
  - Polygonal Mesh
  - Subdivision
  - Parametric
  - Implicit
- Solids
  - Voxels
  - BSP tree
  - CSG
  - Sweep
- High-level structures
  - Scene graph
  - Application specific

# Equivalence of Representations

- Thesis:
  - Each representation has enough expressive power to model the shape of any geometric object
  - It is possible to perform all geometric operations with any fundamental representation
- Analogous to Turing-equivalence
  - Computers / programming languages Turing-equivalent. But each does different things better!

# Why different Representations?

- Efficiency for different tasks
  - Acquisition
  - Rendering
  - Manipulation
  - Animation
  - Analysis

Data Structures determine algorithms!

# Modeling Operations

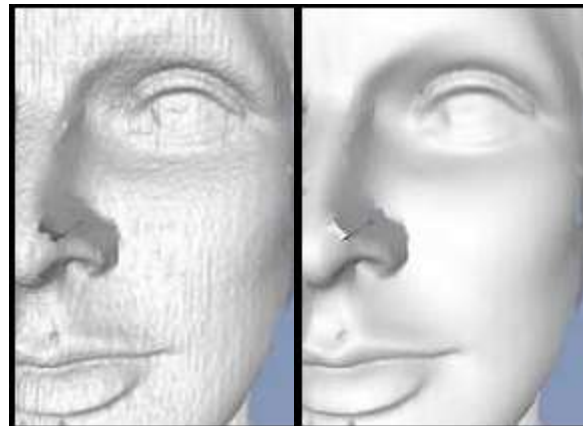
- What can we do with a 3D object representation?
  - Edit
  - Transform
  - Smooth
  - Render
  - Animate
  - Morph
  - Compress
  - Transmit
  - Analyze
  - ...



Digital Michealangelo



Pirates of the carribeian



Smoothing



# 3D Object Representations

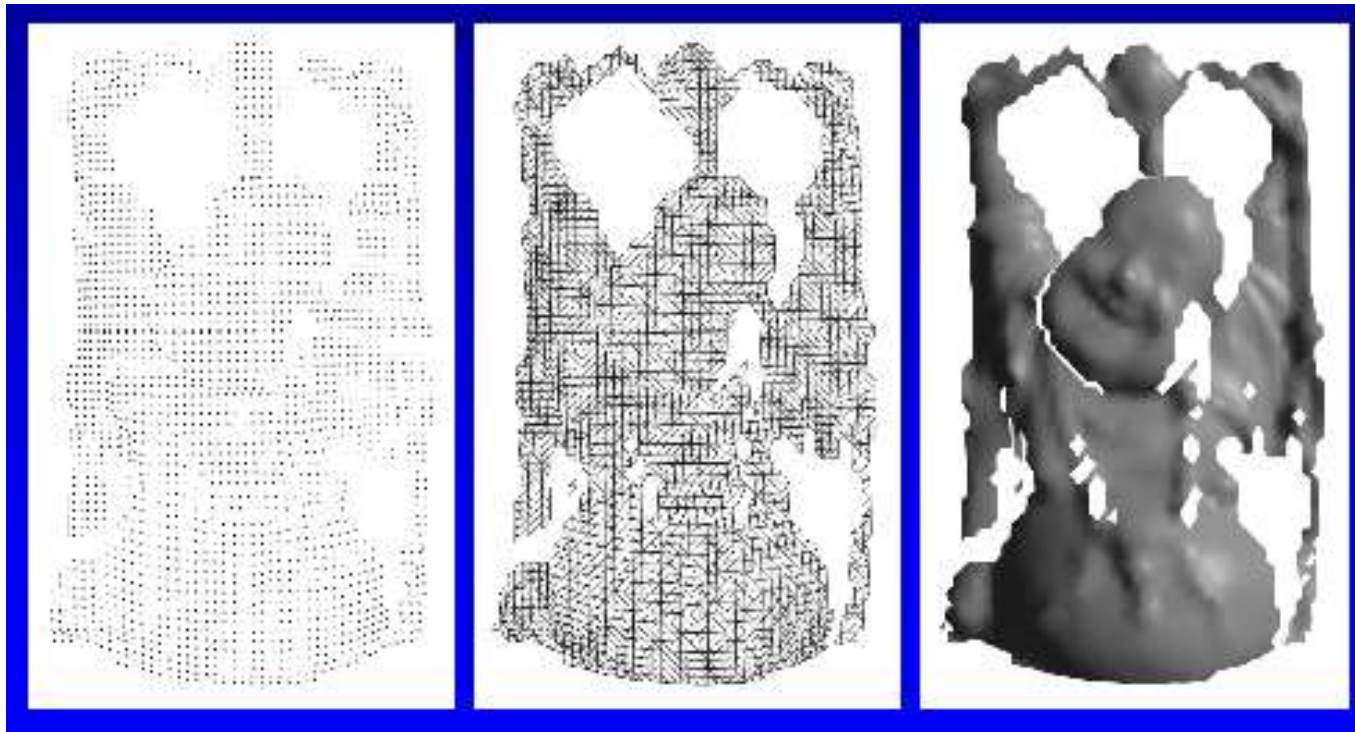
- Desirable properties depend on intended use
  - Easy to acquire
  - Accurate
  - Concise
  - Intuitive editing
  - Efficient editing
  - Efficient display
  - Efficient intersections
  - Guaranteed validity
  - Guaranteed smoothness
  - ...

# Outline

- Points
  - Point cloud
  - Range image
- Surfaces
  - Polygonal Mesh
  - Subdivision
  - Parametric
  - Implicit
- Solids
  - Voxels
  - BSP tree
  - CSG
  - Sweep
- High-level structures
  - Scene graph
  - Application specific

# Range Image

- Set of 3D points mapping to pixels of depth image
  - Acquired from range scanner



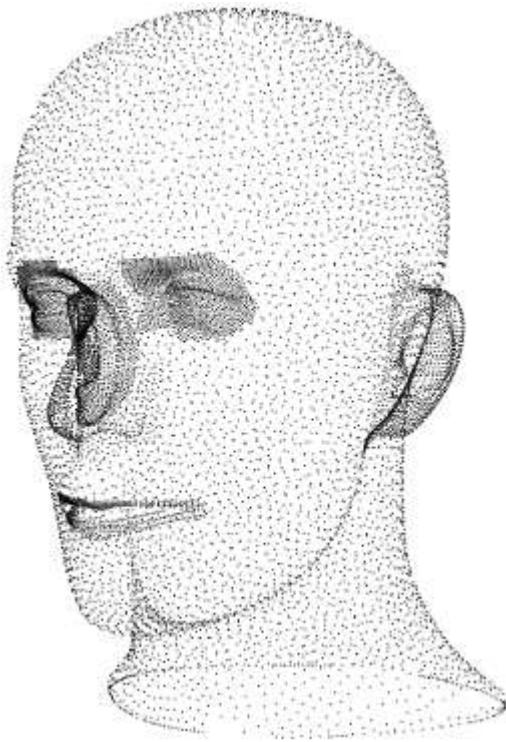
Range Image

Tessellation

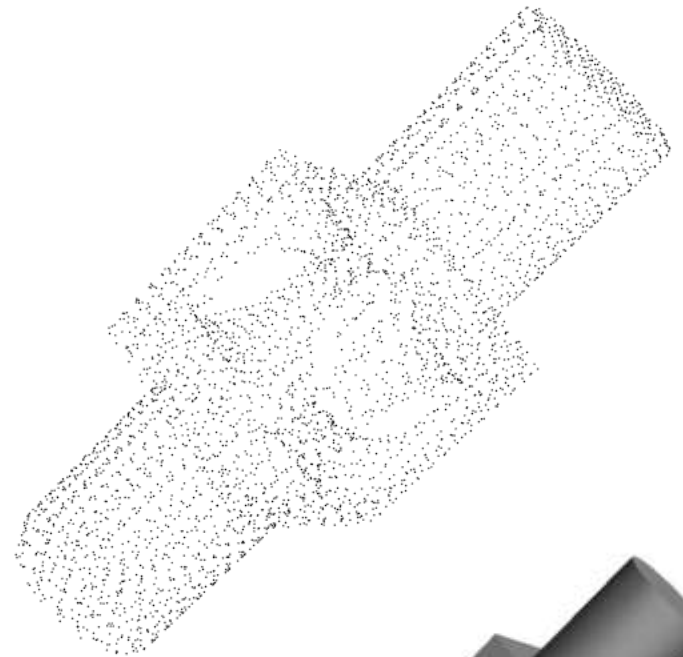
Range Surface

# Point Cloud

- Unstructured set of 3D point samples
  - Acquired from range finder, computer vision, etc



Hugues Hoppe



Hugues Hoppe



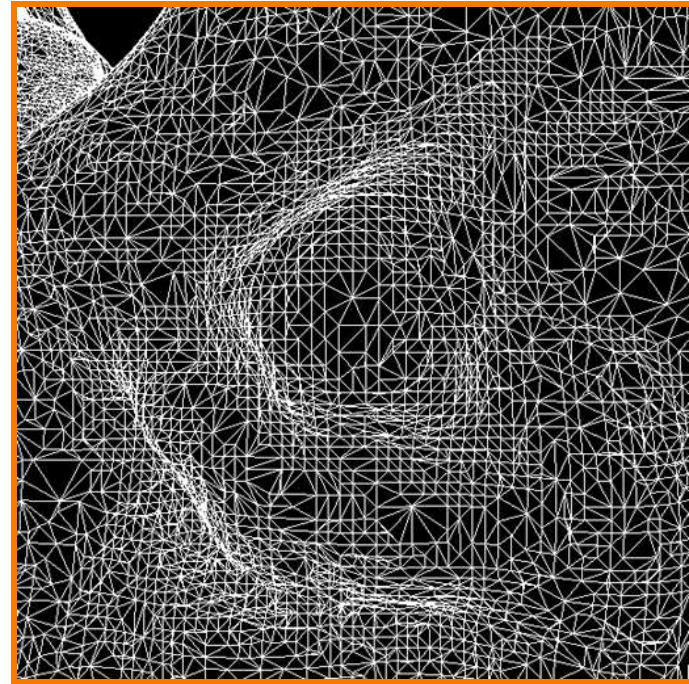


# Outline

- Points
  - Point cloud
  - Range image
- Surfaces
  - Polygonal Mesh
  - Subdivision
  - Parametric
  - Implicit
- Solids
  - Voxels
  - BSP tree
  - CSG
  - Sweep
- High-level structures
  - Scene graph
  - Application specific

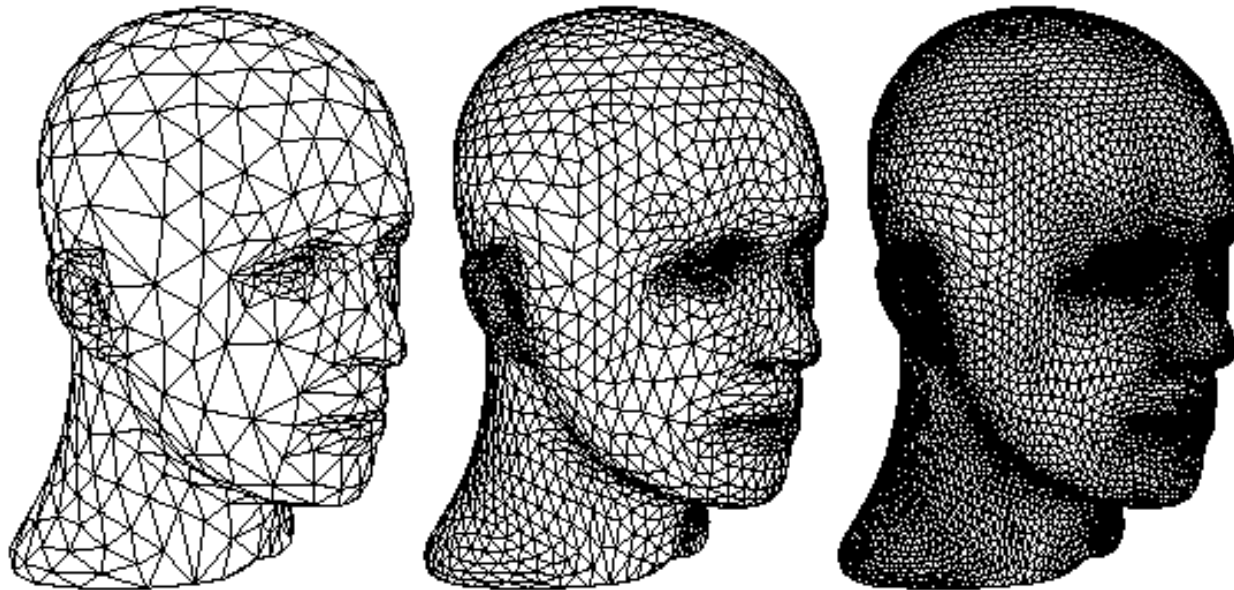
# Polygonal Mesh

- Connected set of polygons (usually triangles)



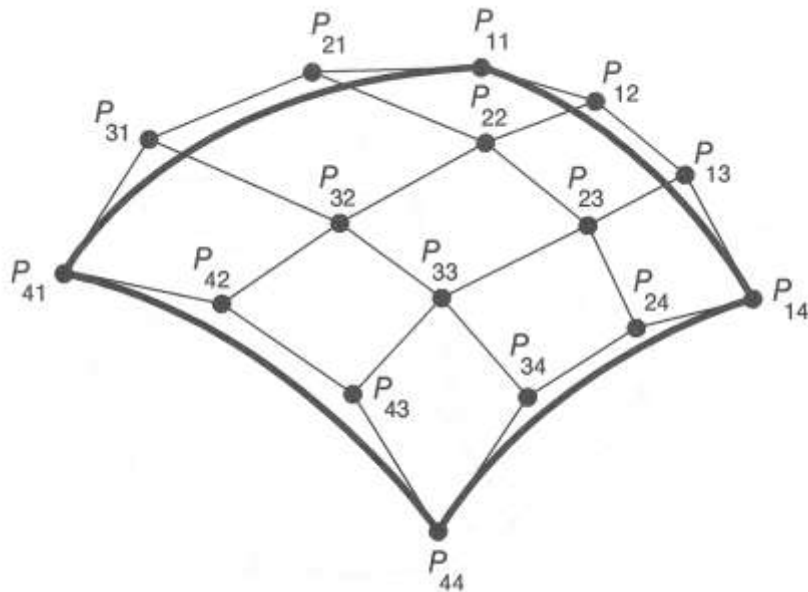
# Subdivision Surface

- Coarse mesh & subdivision rule
  - Define smooth surface as limit of sequence of refinements

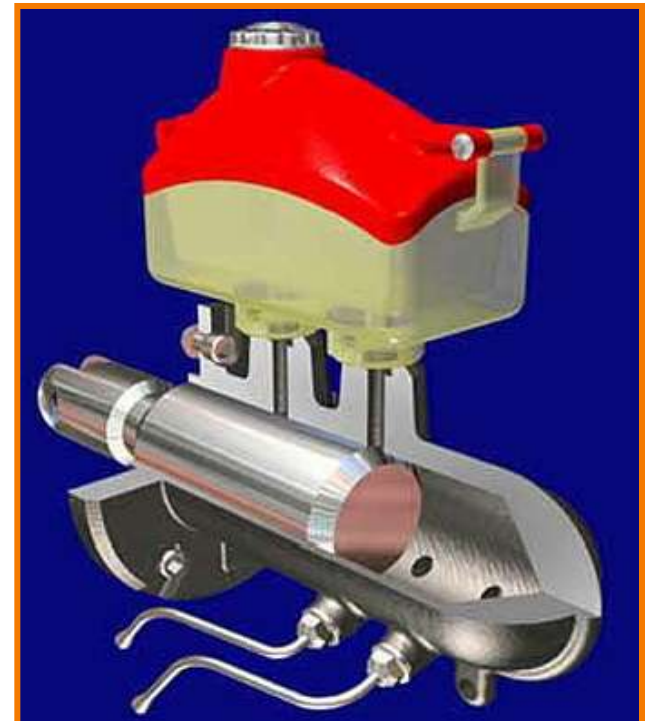


# Parametric Surface

- Tensor product spline patches
  - Each patch is a parametric function
  - Careful constraints to maintain continuity



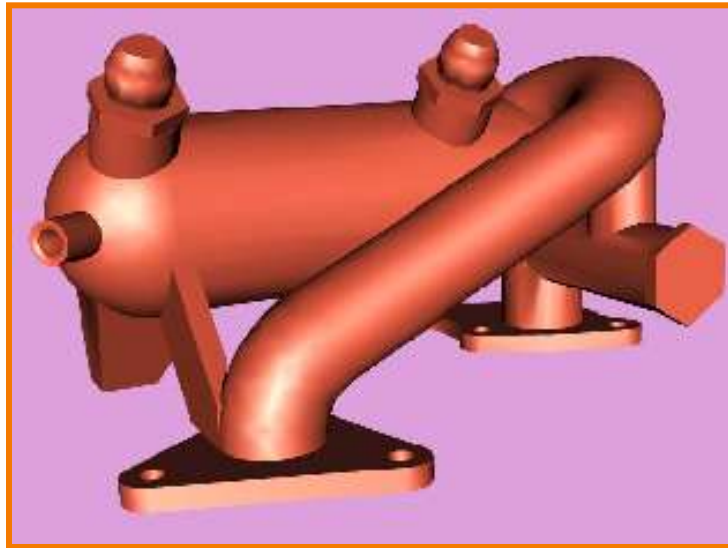
FvDFH Figure 11.44



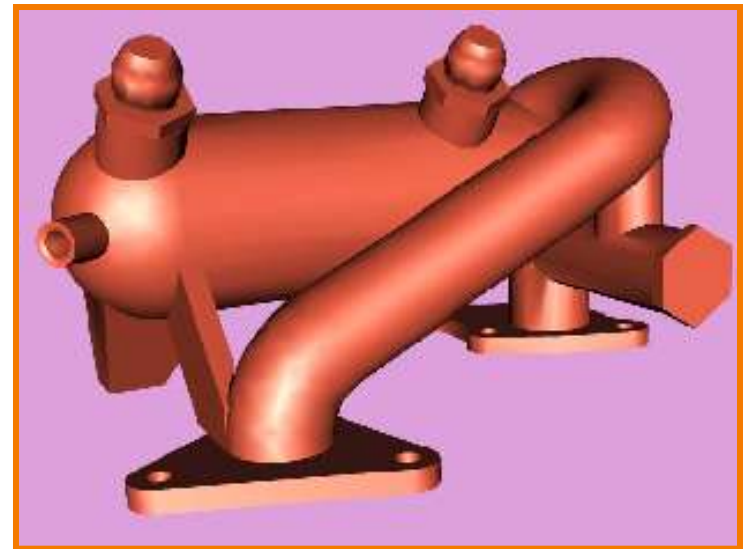


# Implicit Surface

- Points satisfying:  $F(x,y,z) = 0$



Polygonal Model



Implicit Model

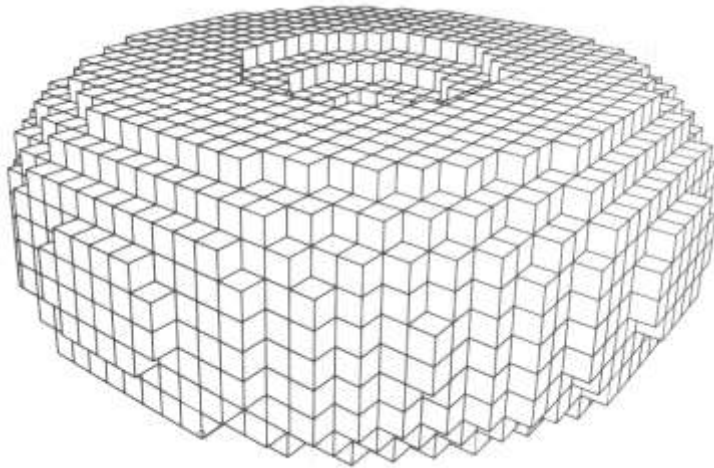
Bill Lorensen  
SIGGRAPH 99  
Course #4 Notes

# Outline

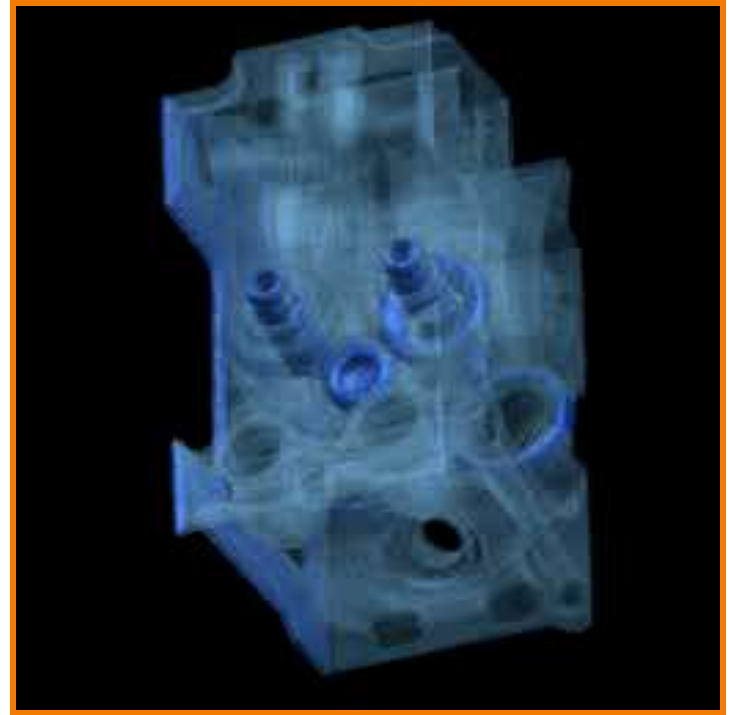
- Points
  - Point cloud
  - Range image
- Surfaces
  - Polygonal Mesh
  - Subdivision
  - Parametric
  - Implicit
- Solids
  - Voxels
  - BSP tree
  - CSG
  - Sweep
- High-level structures
  - Scene graph
  - Application specific

# Voxels

- Uniform grid of volumetric samples
  - Acquired from CAT, MRI, etc.



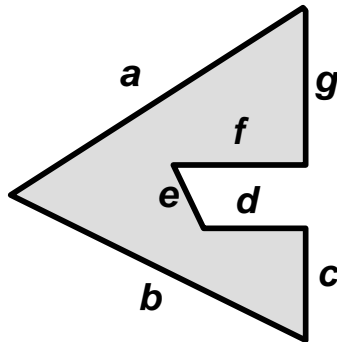
FvDFH Figure 12.20



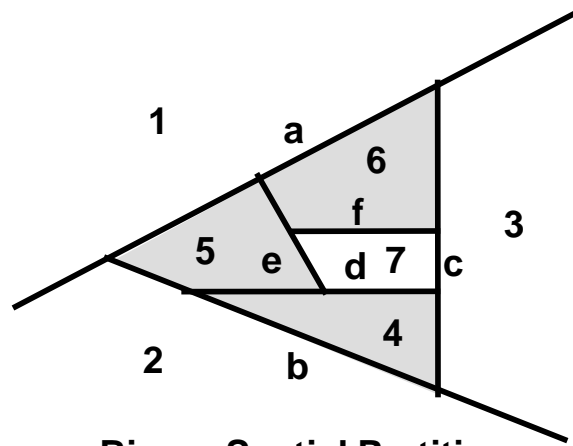
Stanford Graphics Laboratory

# BSP Tree

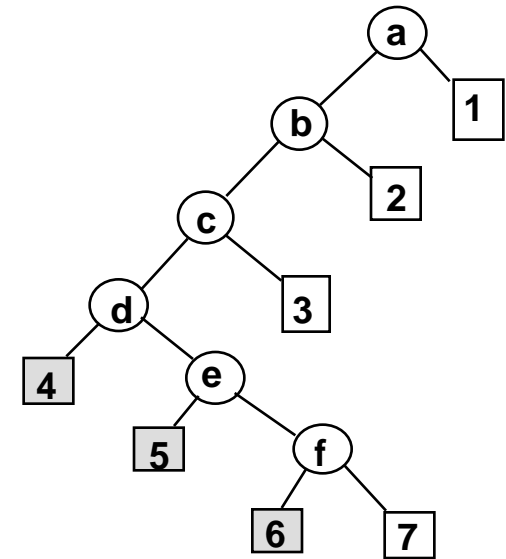
- Binary space partition with solid cells labeled
  - Constructed from polygonal representations



Object



Binary Spatial Partition

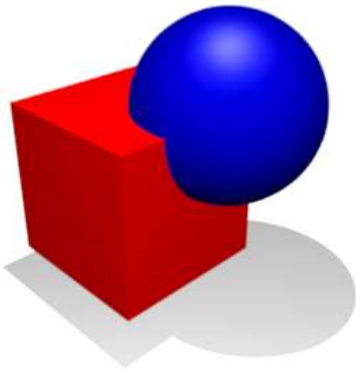


Binary Tree

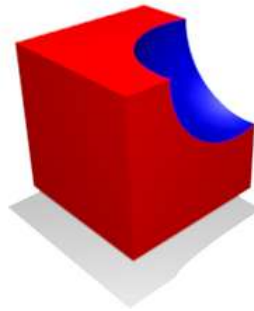
# CSG (constructive solid geometry)

- Hierarchy of boolean set operations (union, difference, intersect) applied to simple shapes

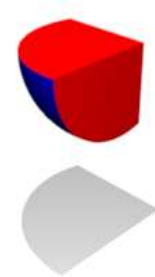
Boolean union



Boolean difference



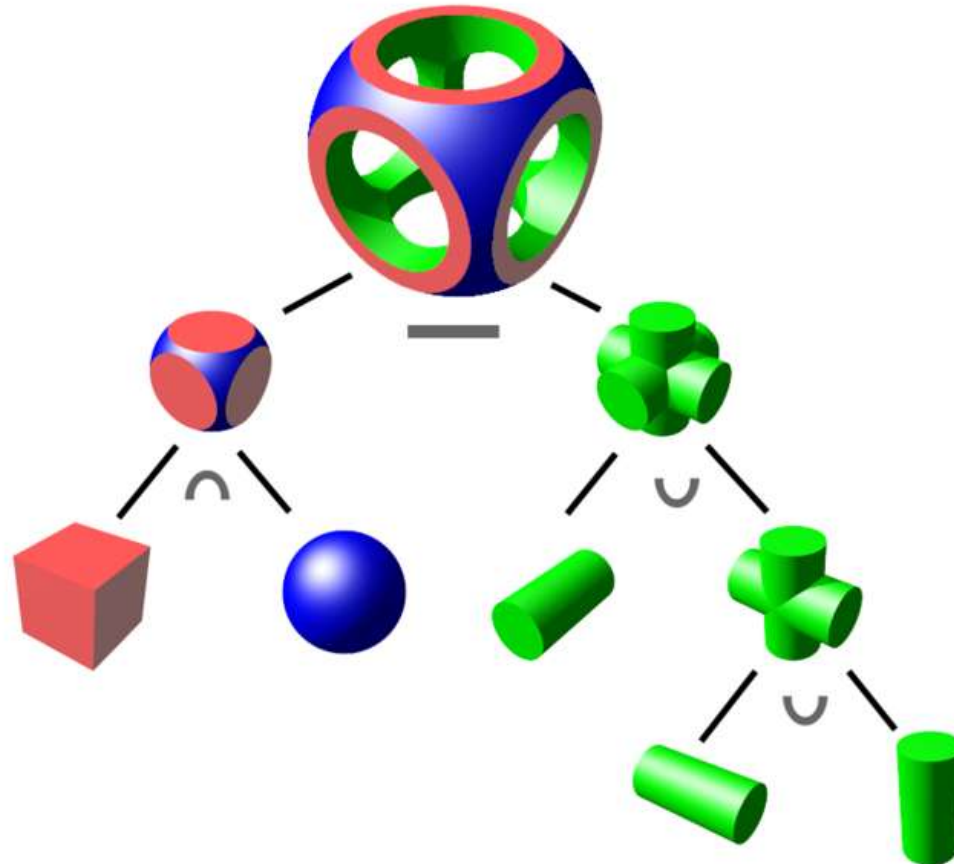
Boolean intersection





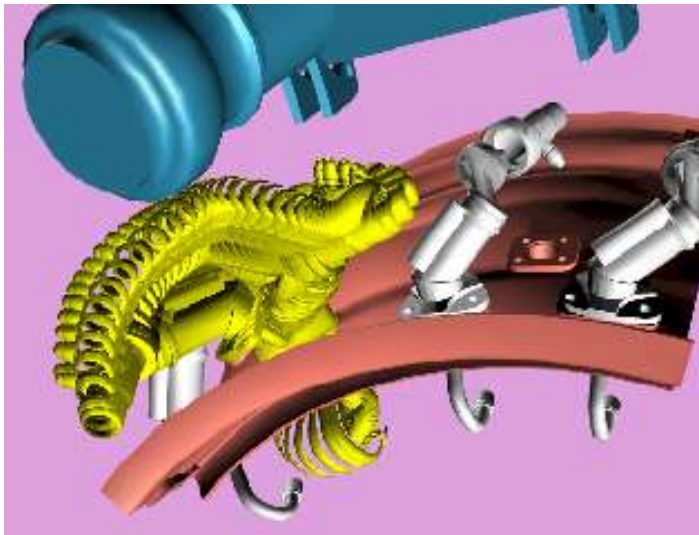
# CSG (constructive solid geometry)

- Hierarchy of boolean set operations (union, difference, intersect) applied to simple shapes

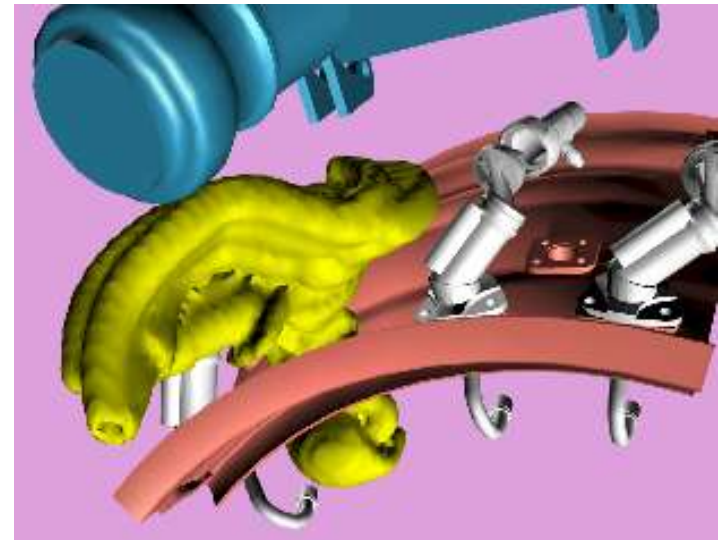


# Sweep

- Solid swept by curve along trajectory



Removal Path



Sweep Model

# Outline

- Points
  - Point cloud
  - Range image
- Surfaces
  - Polygonal Mesh
  - Subdivision
  - Parametric
  - Implicit
- Solids
  - Voxels
  - BSP tree
  - CSG
  - Sweep
- High-level structures
  - Scene graph
  - Application specific

# Scene Graph

- Union of objects at leaf nodes

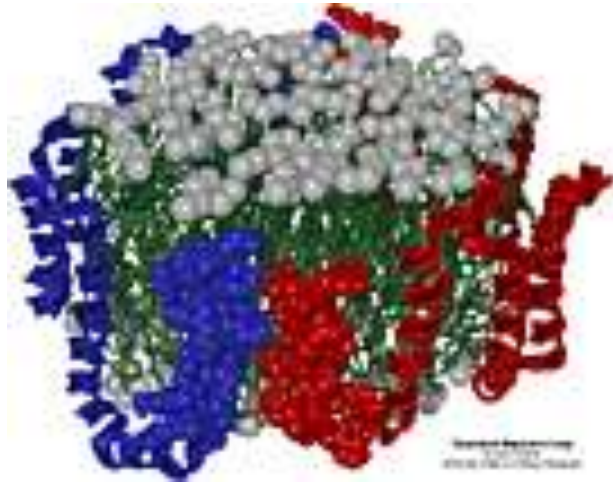


Bell Laboratories



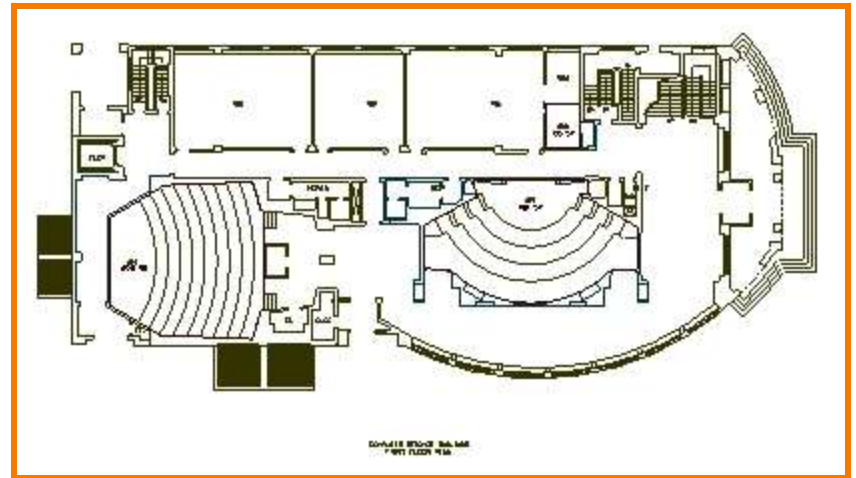
[avalon.viewpoint.com](http://avalon.viewpoint.com)

# Application Specific



Apo A-1

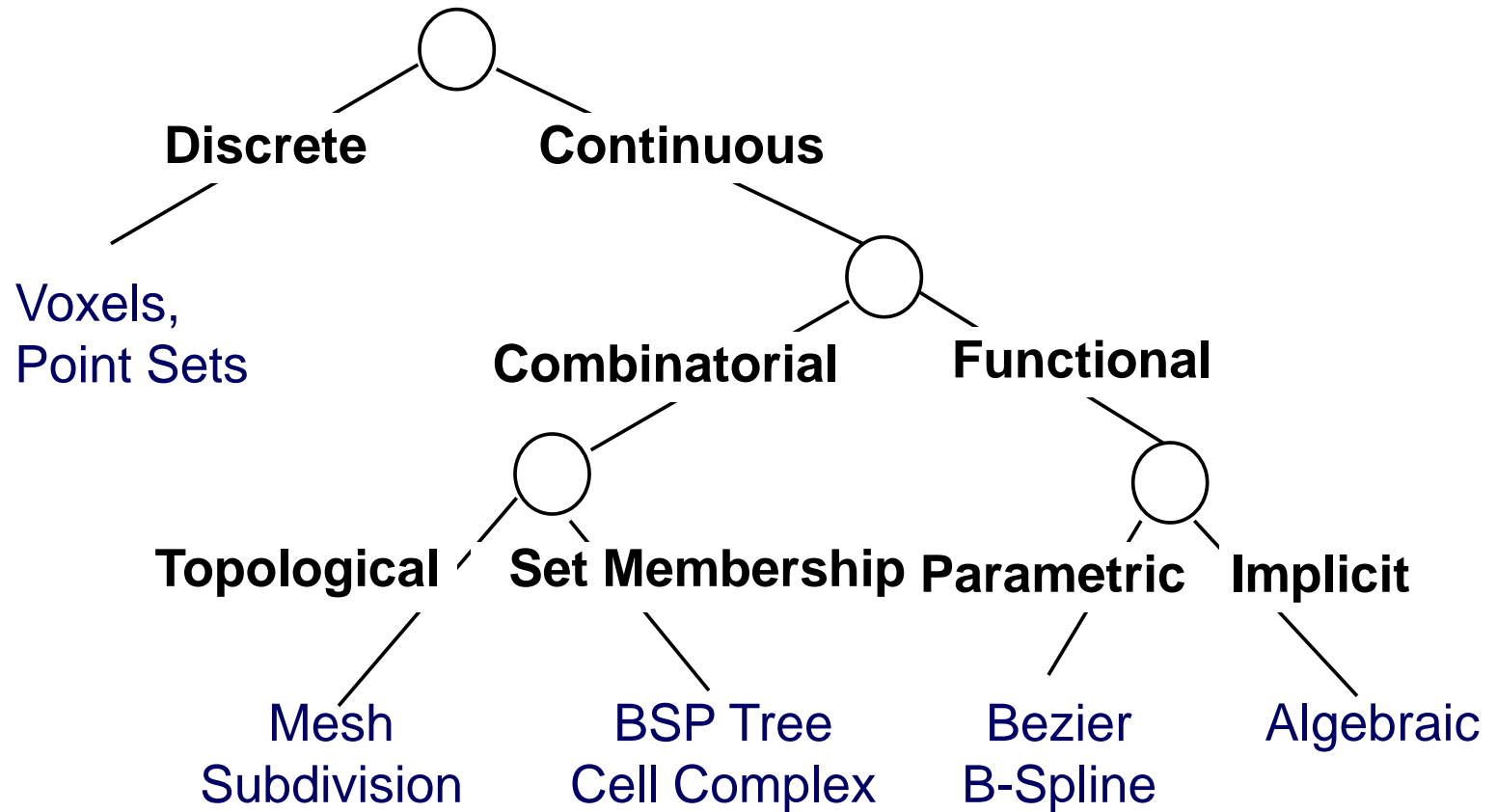
*(Theoretical Biophysics Group,  
University of Illinois at Urbana-Champaign)*



Architectural Floorplan  
*(CS Building, Princeton University)*



# Taxonomy of 3D Representations



# Equivalence of Representations

- Thesis:
  - Each representation has enough expressive power to model the shape of any geometric object
  - It is possible to perform all geometric operations with any fundamental representation
- Analogous to Turing-equivalence
  - Computers / programming languages Turing-equivalent. But each does different things better!

# Computational Differences

- Efficiency
  - Combinatorial complexity (e.g.  $O(n \log n)$ )
  - Space/time trade-offs (e.g. z-buffer)
  - Numerical accuracy/stability (degree of polynomial)
- Simplicity
  - Ease of acquisition
  - Hardware acceleration
  - Software creation and maintenance
- Usability
  - Designer interface vs. computational engine